MAA Metro NY October 2025

Problem of the Month

Proposed by Dr. Asher Roberts, Saint Joseph University

The Problem:

Write the infinite sum

$$1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \frac{1}{25} + \frac{1}{36} + \cdots$$

as an infinite product of fractions of the form $\frac{n}{m}$, where n and m are different numbers in each fraction, but always satisfy n=m+1.