MAA Metro NY July 2025, Problem of the Month

Prove that a triangle with vertices p, q and r in the complex plane is equilateral if and only if $p^2+q^2+r^2-pq-pr-qr=0$.

Computer or AI assisted/generated solutions will not be accepted.