Problem of the Month - May 2024

Show that for $a \ge e$, there exists at least one line that is simultaneously tangent to both $f(x) = a^x$ and $g(x) = \log_a x$.