Imagine a pyramid with a square $2N \times 2N$ base and altitude $N$. Suppose that a cube were placed inside this pyramid so that its upper four corners were situated on the lines where neighboring faces of the pyramid met. Now inscribe a sphere inside this cube. Find the volume of this sphere in terms of $N$. 