

By Apr 20 please

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ABSTRACT OF PAPER

Title of Paper: A modified Runge-Kutta
solution of ordinary differential
equations.

Time.....minutes.

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ABSTRACT

The abstract should be in the form of a brief and concise statement of the main results or points of view of the paper, without demonstrations and with a minimum of formulae. It should not exceed 100 words and should be compressed if possible into a single paragraph. It should be written in the third person. The abstract should be typewritten and in a form suitable for immediate publication in the MONTHLY.

Suppose it is required that a particular solution to the differential equation

$$\frac{dy}{dx} = F(x,y)$$

be found. Suppose further that the points (x_{n-1}, y_{n-1}) and (x_n, y_n) lie on the particular solution curve and that they are given. Let $x_n + h = x_{n+1}$, $y_n + k = y(x_{n+1}) = y_{n+1}$. Here h , the step-size is fixed. Therefore, k , the change in y , must be evaluated to find the next point, (x_{n+1}, y_{n+1}) , on the particular solution curve. The set of equations

$$\begin{aligned} (1) \quad k_0^{(n-1)} &= hF(x_{n-1}, y_{n-1}), \\ (2) \quad k_1^{(n-1)} &= hF(x_{n-1} + uh, y_{n-1} + uk_0^{(n-1)}), \\ (3) \quad k_0^{(n)} &= hF(x_n, y_n), \\ (4) \quad k_1^{(n)} &= hF(x_n + uh, y_n + uk_0^{(n)}), \\ (5) \quad k^{(n)} &= a_0 k_0^{(n)} + a_1 k_1^{(n)} + b_0 k_0^{(n-1)} + b_1 k_1^{(n-1)}, \\ (6) \quad y_{n+1} &\doteq y_n + k^{(n)}, \\ (7) \quad b_0 &= \frac{5-6u}{12u}, \quad (8) \quad b_1 = \frac{-5}{12u} \\ (9) \quad a_0 &= \frac{18u-5}{12u}, \quad (10) \quad a_1 = \frac{5}{12u}, \end{aligned}$$

describes a modified Runge-Kutta method of numerical integration, which has an accuracy of the order of h^3 and which requires only two substitutions into the differential equation for each step of integration. The value of u is dependent upon h and the differential equation.